



The Hong Kong University of Science and Technology

Department of Mathematics

Hong Kong Geometry Colloquium

Point-arrangements in the real projective spaces  
and the Fibonacci polynomials

By

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Abstract

In this report, arrangements of  $n + 2$  points in general position in the real projective  $n$ -space are unique up to projective transformations. Those of  $m := n + 3$  points are projectively not unique, but they are combinatorially unique. We are interested in arrangements of  $m$  points which admit an action of the cyclic group of order  $m$ .

Let  $p_1, \dots, p_{n+2}$  be  $n + 2$  points in general position. We add another point  $p_m$  and require that the  $m$  points  $p_1, \dots, p_{n+2}, p_m$  admit a projective transformation  $\sigma$  inducing the cyclic permutation:

$$\sigma : p_1 \rightarrow p_2 \rightarrow \dots \rightarrow p_{n+2} \rightarrow p_m \rightarrow p_1$$

There always exist such  $p_m$  and  $\sigma$ , and in fact there are several choices in general. We show that such choices exactly correspond to the roots of the *Fibonacci polynomial*  $F_n(t)$  of degree  $[n/2] + 1$ . And moreover, the resulting  $m$  points  $p_1, \dots, p_{n+2}, p_m$  are in general position if and only if the corresponding root is "primitive", i.e., a root of the *core Fibonacci polynomial*  $f_n(t)$ , which is an irreducible factor of  $F_n(t)$  of degree  $\varphi(m)/2$ . Here,  $\varphi(m)$  denoted Euler's function counting the number of positive integers less than  $m$  and co-prime to  $m$ .

**Date** : *Saturday, 10 February 2018*

**Time** : *10:00a.m.-11:00a.m.*

**Venue** : *Room 4504, Academic Building  
(near Lifts 25&26), HKUST*

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**Admissible height pairings of algebraic cycles**

By

*Prof. Shouwu ZHANG*

*Princeton University and IAS of HKUST*

Abstract

For a smooth and projective variety  $X$  over a global field of dimension  $n$  with an adelic polarization, we propose canonical local and global height pairings for two cycles  $Y, Z$  of pure dimension  $p, q$  satisfying  $p+q=n-1$ . We will give some explicit arichmedean local pairings by writing down explicit formula for the diagonal Green current for some Shimura varieties.

**Date** : *Saturday, 10 February 2018*

**Time** : *11:20a.m.-12:20p.m.*

**Venue** : *Room 4504, Academic Building  
(near Lifts 25&26), HKUST*

*All are welcome!*

*Light refreshment will be provided at Room 3493 from 11:00 am to 11:20 am*