



**The Hong Kong University of Science & Technology**

**Department of Mathematics**

**PhD Student Seminar**

**Asymptotic Theory of  
Sparse Bradley-Terry Model**

By

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**Abstract**

Studies of sparse paired comparisons in a large network arouse considerable research interests in recent years. For instance, we can consider a huge social network or large-scale online games. Ranking in these networks has many applications. However in these cases, paired comparisons among users are quite sparse. The Bradley-Terry model is widely used to estimate merits of subjects in the paired comparison. We prove the asymptotic theory of maximum likelihood estimation of Bradley-Terry model with sparse data. Specifically, our asymptotic theorem holds as the sparse probability is larger than or equal to  $\frac{\log^3 t}{t}$  (Latex:  $(\log t)^3/t$ ) for  $t$  subjects. Numerical studies further support our results.

***Date: Monday, 7 May 2018***

***Time: 4:00 p.m.- 5:00 p.m.***

***Venue: Room 4475 (near lift 25, 26)***

***All are welcome!***