



THE HONG KONG UNIVERSITY OF SCIENCE & TECHNOLOGY

Department of Mathematics

SEMINAR ON APPLIED MATHEMATICS

Nonreciprocal Interactions - Drops of Active Liquids and Arrested Coarsening

By

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Abstract

After briefly reviewing the recent effort of physicists and mathematicians alike to break Newton's third law to make systems active [1], we introduce particular continuum models featuring such nonreciprocal interactions that destroy the gradient dynamics structure of well-known models. First, a thin-film model for partially wetting drops on solid substrates is made active by incorporating a nonreciprocal coupling to a polarisation field in the form of self-propulsion and active stress [2]. We show that the employed polarisation-surface coupling results in (hysteretic) transitions between resting and moving drops, the splitting of drops, and chiral motion. Second, we introduce a nonreciprocal Cahn-Hilliard model [3,4], show that all its linear stability thresholds may be mapped onto the ones of a Turing reaction-diffusion system [4], and indicate how the nonreciprocal interactions arrest and stop coarsening, and give rise to localised and/or oscillatory states [4]. Finally, we argue that the nonreciprocal Cahn-Hilliard model indeed is of universal importance as it corresponds to the last missing amplitude equation out of eight that should exist if considering a classification of linear instabilities of uniform constant states based on three features: small- vs large-scale, stationary vs. oscillatory, and with vs. without conservation law [5]. The talk ends with a brief outlook.

References

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3. Z. H. You, A. Baskaran, and M. C. Marchetti, *Proc. Natl. Acad. Sci. U. S. A.* 117, 19767 (2020); S. Saha, J. Agudo-Canalejo, and R. Golestanian, *Phys. Rev. X* 10, 041009 (2020);
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Date : 8 May 2023 (Monday)

Time : 4:30pm – 5:30pm

Venue : Room 4475 (Lifts 25/26)

All are Welcome!