



**THE HONG KONG UNIVERSITY OF SCIENCE & TECHNOLOGY**

**Department of Mathematics**

**SEMINAR ON APPLIED MATHEMATICS**

**No existence of a linear algorithm  
for Fourier phase retrieval**

**By**

**Prof. Zhiqiang XU**

Academy of Mathematics and System Science,  
Chinese Academy of Sciences, Beijing

**Abstract**

Fourier phase retrieval, which aims to reconstruct a signal from its Fourier magnitude, is of fundamental importance in engineering and scientific fields. In this talk, we provide a theoretical understanding of algorithms for the one-dimensional Fourier phase retrieval problem. Specifically, we demonstrate that if an algorithm exists that can reconstruct an arbitrary signal  $\{x\} \in \mathbb{C}^N$  in  $\text{Poly}(N) \log(1/\epsilon)$  time to reach  $\epsilon$ -precision from its magnitude of discrete Fourier transform and its initial value  $x(0)$ , then  $\mathcal{P} = \mathcal{NP}$ . This partially elucidates the phenomenon that, despite the fact that almost all signals are uniquely determined by their Fourier magnitude and the absolute value of their initial value  $|x(0)|$ , no algorithm with theoretical guarantees has been proposed in the last few decades. Our proofs employ the result in computational complexity theory that the Product Partition problem is NP-complete in the strong sense.

**Date : 30 May 2024 (Thursday)**

**Time : 3:00p.m.-4:00p.m.**

**Venue : Room 2129C (near Lift 19)**

*All are Welcome!*