



THE HONG KONG UNIVERSITY OF SCIENCE & TECHNOLOGY

Department of Mathematics

PHD STUDENT SEMINAR

**The Incidence Algebra of Polyhedra over
the Minkowski Algebra**

By

Miss Ying CAO

Abstract

Let V be a finite-dimensional vector space over an ordered field F . Let \wp be the poset of relatively open convex polyhedral sets ordered by the face relation. The Minkowski algebra of polyhedra is an F -module generated by indicator functions of polyhedra with Minkowski multiplication defined as $f * g(x) = \sum_{a,b \in F} ab \chi(f^{-1}(a) \cap (x - g^{-1}(b)))$.

By considering the incidence algebra of the poset \wp over the Minkowski algebra and various Möbius inversion formulas, we can prove the Gram-Sommerville, Gauss-Bonnet formulas and their analogs for relatively open convex polyhedra in a fundamental and unified way.

Date : 13 May 2025 (Tuesday)

Time : 3:00pm

Venue : Room 4502 (near Lifts 25/26)

All are Welcome!