



THE HONG KONG UNIVERSITY OF SCIENCE & TECHNOLOGY

Department of Mathematics

SEMINAR ON APPLIED MATHEMATICS

Addressing two fundamental problems in lattice
Boltzmann method for two-phase flows

By

Prof. Zhaoli GUO

Institute of Multidisciplinary Research for Mathematics and Applied Science
Huazhong University of Science and Technology

Abstract

This talk focuses on two fundamental problems in two-phase lattice Boltzmann equation (LBE) methods: (i) spurious velocities in the vicinity of the phase interface, and (ii) the disappearance of small droplets or bubbles.

For the first issue, we provide a rigorous analysis of the discrete balance property of the LBE to identify the structure of force imbalance. A well-balanced LBE (WB-LBE) model is then proposed, which retains the same algorithmic structure as the standard LBE. The WB-LBE is theoretically shown to achieve a discrete equilibrium state, and its well-balance properties are confirmed through simulations of a flat interface problem and droplet system.

For the second issue, we construct an LBE model based on the Cahn–Hilliard phase-field theory, where the Cahn–Hilliard equation employs a singular mobility that acts only near the interface. The equilibrium distribution function includes a free parameter to enable variable (and even zero) mobility. Meanwhile, the equilibrium distribution function for the Navier–Stokes equations is modified to include another free parameter to achieve a large viscosity ratio. Numerical results demonstrate that the singular LBE model reduces numerical dissipation and yields physically acceptable results over large time scales.

Date : 30 April 2026 (Thursday)

Time : 11:00a.m.-12:00noon

Venue : Room 3598 (Lift 27/28)

All are Welcome!